

The use of the SDS form factor for hydrogen has for the most part led to a greater average bond length, as one would hope. The remaining discrepancy between the X-ray and neutron values is less than  $2\sigma$  in each case (for the mean values of several bond lengths, not for some of the individual values). However the fact that the differences are all in the same direction suggests that the SDS form factor is not adequate to correct fully for the short bond lengths and that it will be necessary to resort to non-spherical scattering factors for precise determination of hydrogen atom positions by X-rays. In the following section, we will use only the neutron diffraction values for hydrogen parameters.

### Hydrogen bonding

Hydrogen bonds exist between the base and the chloride ion, between the base and the water molecule, and between the water molecule and chloride ions. The eight N-H $\cdots$ Cl $^-$  hydrogen bonds represent the largest group of this type that has been studied. The interesting hydrogen bond parameters are given in Table 7. In examining this table, the reader should bear in mind that one useful criterion for hydrogen bonding is a hydrogen atom-heavy atom distance that is 0.2 Å or more shorter than the sum of the van der Waals radii (Hamilton & Ibers, 1967). For this purpose we may take the van der Waals radii of H, O, N, and Cl $^-$  as 1.2, 1.4, 1.5, 1.8 Å. The variability in the H $\cdots$ B dis-

tances as well as in the A-H $\cdots$ B angles is worthy of note.

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## On the Structure of Picrotoxin. II. Direct Determination of the Crystal Structure of $\beta$ -Bromopicrotoxinin

BY BODIL JERSLEV AND E. JØLK RAVN-JONSEN

Chemical Laboratory C, The Royal Danish School of Pharmacy, Copenhagen, Denmark

AND JACOB DANIELSEN

Department of Inorganic Chemistry, University of Aarhus, Aarhus C, Denmark

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The crystal structure of  $\beta$ -bromopicrotoxinin,  $C_{15}H_{15}O_6Br$ , has been determined from three-dimensional, visually estimated X-ray data by a direct method. The parameters were refined anisotropically by the full-matrix least-squares method. The space group is  $P4_3$ ,  $a=b=7.14$  Å,  $c=28.74$  Å. The four molecules in the unit cell are roughly spherical and are placed one on top of the other along the  $c$  axis. The molecular geometry is compared to that of the epimeric compound  $\alpha_1$ -bromopicrotoxinin, a molecule of which the absolute configuration is already known from the X-ray crystallographic work of Craven [*Acta Cryst.* (1962), **15**, 387].

### Introduction

Picrotoxin is a crystalline compound which has found use as a drug in the treatment of barbiturate poisoning. The substance is composed of two molecules, picro-

toxinin,  $C_{15}H_{16}O_6$ , and picrotin,  $C_{15}H_{18}O_7$ , of which the former is the physiologically active principle. The interest of two of us (BJ & R-J) in the structure of picrotoxin dates back to about 1950, when the molecular structures of the components were still unknown.

Picrotoxin was mostly described in the literature at that time as a simple mixture of the two components, though Sielisch (1912) had already shown without doubt that picrotoxin is a molecular compound of picrotoxinin and picrotin in the molecular ratio 1:1. Hansen & Jerslev (1954) confirmed Sielisch's results by means of a thermal analysis supplemented by X-ray powder photographs of various mixtures of the two compounds of the system picrotoxinin-picrotin. This work also showed that neither of the components is miscible with the molecular compound in the solid state.

BJ & R-J furthermore prepared  $\beta$ -bromopicrotoxinin and collected single-crystal X-ray data of that compound, from which the space group, unit cell and approximate bromine parameters were determined. An unsuccessful attempt was also made to solve the structure from the three-dimensional Patterson function using the superposition method in a graphical way. Since we had no access to electronic computers at that time, and since Craven (1959) in a preliminary note indicated that he was working on the crystal structure of the isomeric  $\alpha_1$ -bromopicrotoxinin, we stopped our work on the  $\beta$  compound. A full account of Craven's work giving the molecular structure of  $\alpha_1$ -bromopicrotoxinin including the absolute configuration was published subsequently (Craven, 1962).

In 1962, however, one of us (JD) became interested in attempting to solve a non-centrosymmetrical crystal

structure by means of direct methods. The present paper describes the result of the work of JD on the above named X-ray data.

It is our intention in due time to try to solve the crystal structure of picrotoxinin.

### Experimental

$\beta$ -Bromopicrotoxinin was prepared according to Horrmann (1912) by brominating picrotoxin. Recrystallizations from absolute ethanol gave thin, needle-shaped crystals with a pronounced tendency to split in fibres parallel to the needle axis, melting point (determined under the microscope) 287°C, destr. Crystals of another habit having m.p. 294°C, destr. were also seen, apparently an  $\alpha$ -isomer. The melting points agree well with the data of Horrmann (1912) and Carman (1963). Weissenberg photographs showed the  $\beta$ -bromopicrotoxinin crystals to be tetragonal, elongated in the **c** direction.  $a=b=7 \cdot 114 \text{ \AA}$ ,  $c=28 \cdot 74 \text{ \AA}$ . The density was determined as 1.715; the calculated density 1.702 gives  $Z=4$ . Reflexions of all orders were observed except  $00l$ , which were present only for  $l=4$ . This, and the Laue symmetry  $4/m$ , indicate the space group as one of the two enantiomorphs  $P4_1$  and  $P4_3$ . The latter was, after completion of the structure determination, found to be correct. Intensities were registered using Cu  $K\alpha$  radiation and multiple-film techniques. The zones  $0kl-4kl$  were recorded from a crystal fragment of di-

Table 1. Comparison of theoretical and experimental statistics

	Centrosymmetry	Non-centrosymmetry	Experimental
$\langle  E ^2 \rangle$	1.000	1.000	0.985
$\langle  E  \rangle$	0.798	0.886	0.898
$\langle  E^2 - 1  \rangle$	0.968	0.736	0.678

Table 2. Final atomic positions in fractions of the cell edges

	$x$	$10^5 \cdot \sigma$	$y$	$10^5 \cdot \sigma$	$z$	$10^5 \cdot \sigma$
Br	0.70056	28	0.81447	28	0.59000	—
O(1)	0.80057	169	0.40744	183	0.54561	38
O(2)	0.97430	253	0.27627	239	0.40599	49
O(3)	1.40085	267	0.29017	225	0.40589	59
O(4)	1.35745	183	0.48357	183	0.46599	49
O(5)	1.27206	239	-0.03330	197	0.51819	70
O(6)	1.36728	183	0.25534	169	0.53571	49
C(1)	1.02641	197	0.44775	197	0.48160	49
C(2)	1.21293	225	0.52444	197	0.50110	49
C(3)	1.27079	225	0.43441	197	0.54770	59
C(4)	1.11152	225	0.36686	225	0.57881	49
C(5)	1.05043	225	0.20239	197	0.54940	59
C(6)	0.92388	197	0.30674	211	0.51400	59
C(7)	0.90239	281	0.60028	253	0.46240	70
C(8)	0.91630	225	0.46840	225	0.58529	70
C(9)	0.82458	225	0.39607	267	0.62899	59
C(10)	0.94607	211	0.68062	197	0.58428	70
C(11)	0.82472	295	0.16714	239	0.47968	59
C(12)	0.97852	281	0.14902	267	0.44230	70
C(13)	1.09200	281	0.31489	253	0.44380	59
C(14)	1.29636	267	0.35534	267	0.43498	70
C(15)	1.23315	295	0.12739	225	0.53191	70

mensions  $a \times b \times c = 0.16 \times 0.16 \times 0.24 \text{ mm}^3$ . Reflexions  $hk0$  were recorded from a crystal fragment with cross section about  $0.2 \times 0.2 \text{ mm}^2$ . The intensities were estimated visually by means of a calibrated scale and converted to a set  $F_{\text{obs}}$  values in the usual way.

$\alpha$ -Chloropicrotoxinin was prepared in an analogous way, and we confirm Craven's (1959) report, that this substance is isomorphous with the bromine compound. We found m.p.  $277^\circ\text{C}$ ,  $a=b=7.09 \text{ \AA}$ ,  $c=29.0 \text{ \AA}$  and density =  $1.50_0$ . The calculated density  $1.49_0$  gives  $Z=4$ .

### Structure determination

The 1247 independent  $F_{\text{h}\bar{\text{o}}\text{s}\bar{\text{b}}}^2$  values were corrected for vibrational motion and placed on an absolute scale by a method described by Hauptman & Karle (1953) and Karle, Hauptman & Christ (1958). These corrected values,  $F_{\text{h}}^2$ , were converted to normalized structure factors using the relation:

$$E_{\text{h}}^2 = F_{\text{h}}^2 / (\varepsilon_{\text{h}} \sum_{j=1}^N f_{jh}^2).$$

Table 3. Final anisotropic parameters

Temperature factor expressed as  $\exp[-2\pi^2(U_{11}h^2a^*+U_{22}k^2b^*+U_{33}l^2c^*+2U_{23}klb^*c^*+2U_{13}lhc^*a^*+2U_{12}hka^*b^*)]$

	$U_{11}$	$\sigma(U_{11})$	$U_{22}$	$\sigma(U_{22})$	$U_{33}$	$\sigma(U_{33})$	$U_{12}$	$\sigma(U_{12})$	$U_{13}$	$\sigma(U_{13})$	$U_{23}$	$\sigma(U_{23})$
Br	0.066	0.001	0.057	0.001	0.092	0.004	0.006	0.001	0.023	0.001	0.000	0.001
O(1)	0.053	0.006	0.053	0.006	0.046	0.004	-0.010	0.006	0.002	0.005	0.006	0.005
O(2)	0.086	0.010	0.085	0.010	0.046	0.008	-0.019	0.009	-0.018	0.006	-0.012	0.006
O(3)	0.090	0.011	0.061	0.008	0.067	0.008	0.011	0.008	0.031	0.009	-0.015	0.006
O(4)	0.053	0.007	0.050	0.006	0.058	0.008	-0.006	0.006	0.011	0.005	-0.009	0.006
O(5)	0.041	0.007	0.075	0.009	0.125	0.013	-0.002	0.007	-0.015	0.010	-0.038	0.008
O(6)	0.046	0.006	0.041	0.006	0.075	0.008	0.014	0.006	-0.006	0.006	-0.011	0.005
C(1)	0.041	0.007	0.029	0.006	0.029	0.004	0.004	0.006	-0.003	0.005	0.001	0.005
C(2)	0.025	0.006	0.057	0.008	0.042	0.008	-0.012	0.006	0.004	0.006	-0.006	0.005
C(3)	0.040	0.008	0.030	0.006	0.050	0.008	-0.005	0.006	0.008	0.006	-0.011	0.006
C(4)	0.046	0.008	0.046	0.008	0.033	0.008	-0.003	0.006	-0.005	0.005	0.006	0.005
C(5)	0.037	0.008	0.037	0.006	0.050	0.008	-0.003	0.006	0.005	0.006	0.001	0.006
C(6)	0.047	0.008	0.037	0.006	0.050	0.008	-0.010	0.006	0.000	0.006	-0.007	0.007
C(7)	0.065	0.011	0.047	0.009	0.046	0.008	0.013	0.008	-0.005	0.009	0.004	0.007
C(8)	0.047	0.008	0.047	0.008	0.046	0.008	-0.011	0.007	-0.005	0.007	-0.001	0.007
C(9)	0.057	0.010	0.046	0.008	0.046	0.008	-0.001	0.008	0.013	0.006	0.010	0.007
C(10)	0.034	0.007	0.033	0.007	0.063	0.008	0.007	0.006	0.007	0.006	-0.012	0.007
C(11)	0.050	0.008	0.084	0.012	0.050	0.008	-0.019	0.008	-0.003	0.008	-0.012	0.007
C(12)	0.053	0.009	0.052	0.010	0.058	0.008	-0.006	0.009	-0.007	0.008	-0.017	0.008
C(13)	0.059	0.009	0.048	0.009	0.046	0.009	-0.006	0.008	0.004	0.007	-0.007	0.007
C(14)	0.053	0.010	0.050	0.009	0.058	0.008	-0.008	0.008	0.011	0.008	0.002	0.008
C(15)	0.070	0.011	0.023	0.006	0.067	0.008	0.010	0.008	-0.007	0.009	-0.007	0.006

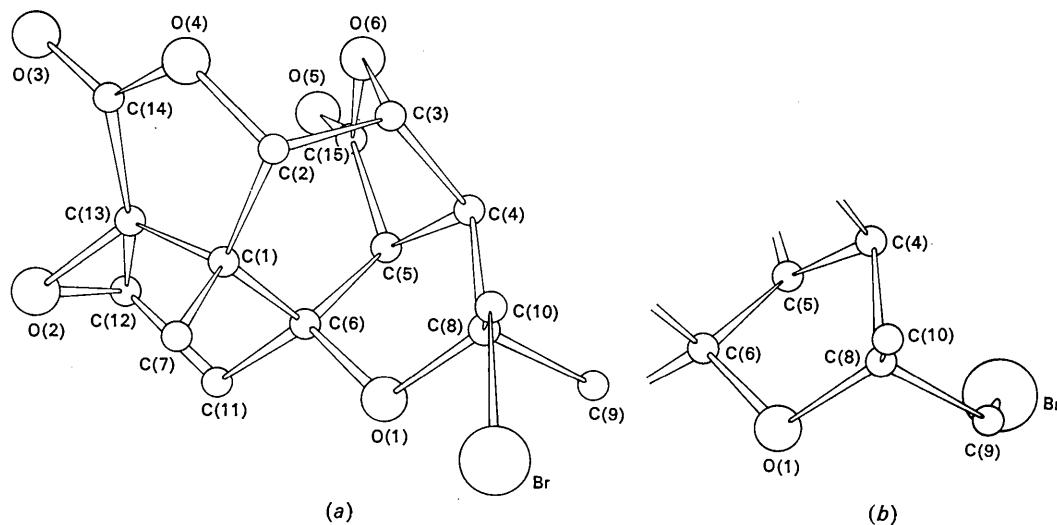


Fig. 1. (a) A molecule of  $\beta$ -bromopicrotoxinin viewed along the  $b$  axis. (b) Approximately correct drawing of part of a molecule of  $\alpha_1$ -bromopicrotoxinin orientated as the epimeric molecule in (a).

$N$  is the total number of atoms in the unit cell,  $\varepsilon_h$  is a weighting factor; in this case  $\varepsilon_h$  was set equal to 1, and  $f_{jh}$  is the appropriate atomic form factors from *International Tables for X-ray Crystallography*, Vol. III, Table 3.3.1A.

Average values of functions of  $E_h$  are compared with the corresponding theoretical values for centrosym-

metric and non-centrosymmetric structures in Table 1. It is seen that the choice of the asymmetric space group  $P4_1$  is in agreement with the statistics described by e.g. Karle, Karle, Owen & Hoard (1965).

From the expression for the joint probability distribution (Naya, Nitta & Oda, 1965) for a set of three structure factors it can be shown that if

Table 4. Observed and calculated structure factors

Columns are: index  $k$ ,  $|F_{\text{obs}}| \times 10^2$ ,  $|F_{\text{calc}}| \times 10^2$ , phase angle in millicycles.

	0, K, 0	4 136 133 38	3 316 390 817	6 88 93 820	1 39 47 174	2 55 60 251	1, K, 3	-5 130 159 10	7 147 106 0	-6 55 59 185	2, K, 14	-4 307 324 993
21002 965 500	6 96 97 703	4 78 86 678	7 232 197 560	4 78 86 650	4 136 130 583	8 124 113 870	-3 239 266 548	7 127 102 0	-6 127 102 0	-3 239 266 687	-8 55 51 337	-3 669 551 542
3 275 225 0	0, K, 24	7 88 85 696	6 242 227 219	5 45 46 594	5 106 84 808	-2 78 99 263	2 111 127 273	3 104 129 267	-6 117 138 758	3 475 492 270	-3 557 510 576	
4 124 129 0	0, K, 24	7 88 85 696	5 55 56 136	5 106 84 808	4 147 180 696	4 59 54 287	5 147 180 696	4 254 398 656	4 254 398 656	4 254 398 656	4 254 398 656	
6 204 148 0	0, K, 24	7 88 85 696	1 107 512 472	7 147 105 297	7 147 105 297	8 -55 61 314	-7 104 154 728	-6 78 88 800	-3 185 220 278	-6 185 220 278	-6 185 220 278	
7 147 157 500	2 124 119 683	0, K, 18	1 375 117 956	2 750 806 438	2 397 448 231	2 397 448 231	2 397 448 231	2 397 448 231	2 397 448 231	2 385 389 216	7 166 163 643	
9 55 51 500	3 88 87 639	1 130 136 646	3 403 386 378	4 171 223 921	4 171 223 921	8 124 113 870	-6 136 154 554	5 124 114 159	3 342 314 284	3 342 314 284	3 342 314 284	
0, K, 4	0, K, 24	3 387 375 142	5 126 131 629	6 215 202 275	2 136 133 626	-6 211 241 576	-6 211 241 576	-6 211 241 576	-6 211 241 576	-6 211 241 576	-6 211 241 576	
8 147 157 500	2 124 119 683	0, K, 24	4 200 196 326	7 239 237 582	3 36 28 293	3 32 343 423	3 211 211 886	4 55 74 637	6 73 85 225	-7 104 130 602	-7 104 130 602	
1 104 120 250	1 88 88 521	5 232 201 645	6 78 193 908	7 104 103 890	7 104 103 890	8 55 61 314	-7 104 154 728	-6 78 88 800	2 385 389 216	7 166 163 643	7 166 163 643	
2 210 180 650	2 85 88 520	7 95 60 103	7 175 202 645	8 55 61 314	8 55 61 314	8 55 61 314	8 55 61 314	8 55 61 314	8 55 61 314	8 55 61 314	8 55 61 314	
3 184 217 663	3 95 66 302	0, K, 13	1 107 311 73 81	1 107 311 73 81	1 107 311 73 81	2 405 370 413	-7 175 702 91	-39 55 303	3 342 314 284	3 342 314 284	3 342 314 284	
4 104 105 152	4 39 88 574	0, K, 24	1 407 495 339	2 520 548 747	1 117 127 273	3 497 454 554	3 497 454 554	3 497 454 554	3 497 454 554	3 497 454 554	3 497 454 554	
5 55 51 500	6 55 50 383	0, K, 24	2 406 502 225	3 473 487 521	3 45 47 261	5 312 241 977	-7 130 141 637	5 79 73 963	-6 78 102 147	-3 175 172 333	-3 175 172 333	
6 147 157 500	6 55 50 383	0, K, 24	3 182 181 486	4 525 514 284	5 166 163 626	6 88 113 503	6 88 113 503	6 88 113 503	6 88 113 503	6 88 113 503	6 88 113 503	
7 55 51 500	6 55 50 383	0, K, 24	5 182 181 486	4 525 514 284	5 166 163 626	6 88 113 503	6 88 113 503	6 88 113 503	6 88 113 503	6 88 113 503	6 88 113 503	
8 147 143 850	3 25 66 477	9 104 23 56	1 117 97 610	7 104 103 890	7 104 103 890	8 55 61 314	-7 104 154 728	-6 78 88 800	2 196 209 500	2 196 209 500	2 196 209 500	
9 124 143 850	3 39 28 771	0, K, 8	7 78 76 332	8 55 68 116	8 55 68 116	8 55 68 116	8 55 68 116	8 55 68 116	8 55 68 116	8 55 68 116	8 55 68 116	
0, K, 8	0, K, 24	0, K, 24	7 78 76 332	8 55 68 116	8 55 68 116	8 55 68 116	8 55 68 116	8 55 68 116	8 55 68 116	8 55 68 116	8 55 68 116	
1 3 3 8 894	0, K, 16	1 70 78 92 731	0, K, 17	1 70 78 92 731	0, K, 17	1 70 78 92 731	0, K, 17					
2 196 199 109	1 723 859 479	2 117 128 205	0, K, 17	1 70 78 92 731	0, K, 17	1 70 78 92 731	0, K, 17					
3 347 319 323	2 509 526 189	3 132 128 845	0, K, 17	1 70 78 92 731	0, K, 17	1 70 78 92 731	0, K, 17					
4 200 180 250	3 132 128 845	3 132 128 845	0, K, 17	1 70 78 92 731	0, K, 17	1 70 78 92 731	0, K, 17					
5 105 165 143	6 124 182 733	5 116 121 273	2 102 126 272	3 111 121 273	1 629 676 500	4 78 75 519	-5 34 29 209	3 104 129 303	6 165 140 303	-6 104 130 303	-6 104 130 303	
6 257 270 736	5 657 570 214	6 139 27 327	3 111 121 273	3 111 121 273	3 111 121 273	3 424 426 783	-3 78 80 245	6 235 293 201	6 235 293 201	-6 249 286 576	-6 249 286 576	
7 3 31 152 152	6 117 132 112	0, K, 30	4 250 237 335	4 500 508 613	4 166 163 626	5 312 241 977	-7 130 141 637	5 79 73 963	-6 78 102 147	-3 175 172 333	-3 175 172 333	
8 124 137 211	7 88 103 847	0, K, 30	4 250 237 335	4 500 508 613	4 166 163 626	6 693 632 602	2 136 128 68	6 136 128 68	6 136 128 68	6 136 128 68	6 136 128 68	
9 96 123 510	7 131 121 112	0, K, 30	4 250 237 335	4 500 508 613	4 166 163 626	6 693 632 602	2 136 128 68	6 136 128 68	6 136 128 68	6 136 128 68	6 136 128 68	
0, K, 12	0, K, 24	1 88 85 851	7 55 56 134	7 141 20 364	7 39 51 0	3 554 561 588	3 104 116 226	6 136 128 68	6 136 128 68	6 136 128 68	6 136 128 68	
1 242 258 143	0, K, 16	2 78 76 332	7 55 56 134	8 39 20 619	9 39 10 0	5 166 163 626	4 55 64 455	8 78 88 748	-7 80 88 748	-7 80 88 748	-7 80 88 748	
2 375 490 645	1 351 304 247	5 96 86 645	0, K, 21	0, K, 15	0, K, 15	6 130 118 180	-4 147 140 493	6 105 120 327	5 155 125 168	5 155 125 168	5 155 125 168	
3 130 138 112	2 737 620 988	4 222 222 336	0, K, 34	1 111 121 951	1 291 321 618	8 39 40 660	8 55 68 120	2 204 207 212	5 375 285 485	5 375 285 485	5 375 285 485	
4 152 157 221	4 222 222 336	4 222 222 336	0, K, 34	2 202 205 729	2 104 117 224	-7 88 52 576	3 29 55 312	3 130 144 634	-5 242 266 83	-5 242 266 83	-5 242 266 83	
5 210 620 221	4 130 108 524	5 116 121 273	2 102 126 272	3 111 121 273	1 629 676 500	4 78 75 519	-5 34 29 209	3 104 129 303	6 165 140 303	-6 104 130 303	-6 104 130 303	
6 162 168 25	5 419 451 547	1 55 58 129	3 229 208 445	3 166 163 626	-6 200 233 397	4 9 115 351	-5 34 29 209	3 104 129 303	6 165 140 303	-6 104 130 303	-6 104 130 303	
7 3 37 214 227	6 130 132 564	5 55 56 151	4 147 152 482	3 166 163 626	3 166 163 626	8 39 47 914	3 39 52 653	4 124 113 273	5 167 143 377	5 167 143 377	5 167 143 377	
8 96 123 510	7 131 121 112	0, K, 16	8 39 47 914	3 166 163 626	3 166 163 626	8 130 114 990	-4 31 47 910	7 104 121 73	4 124 113 273	5 167 143 377	5 167 143 377	
0, K, 12	0, K, 24	0, K, 24	8 39 47 914	3 166 163 626	3 166 163 626	8 130 114 990	-4 31 47 910	7 104 121 73	4 124 113 273	5 167 143 377	5 167 143 377	
1 78 88 156	2 419 416 510	2 125 222 336	0, K, 16	1 70 78 92 731	1 70 78 92 731	2 399 431 981	2 399 431 981	2 399 431 981	2 399 431 981	2 399 431 981	2 399 431 981	
2 309 329 986	1 312 331 98	2 375 274 848	2 105 112 205	0, K, 19	3 417 466 316	1 157 179 740	-7 78 92 912	2 399 431 981	2 399 431 981	2 399 431 981	2 399 431 981	
3 147 147 223	2 130 147 525	4 168 206 977	3 122 132 766	0, K, 19	4 691 476 316	3 497 454 554	2 399 431 981	2 399 431 981	2 399 431 981	2 399 431 981	2 399 431 981	
4 123 143 651	3 130 147 525	4 168 206 977	3 122 132 766	0, K, 19	4 691 476 316	3 497 454 554	2 399 431 981	2 399 431 981	2 399 431 981	2 399 431 981	2 399 431 981	
5 231 194 405	4 88 95 760	2 105 112 205	1 215 235 397	5 175 197 764	6 235 199 572	4 9 115 351	-5 34 29 209	3 104 129 303	6 165 140 303	-6 104 130 303	-6 104 130 303	
6 88 91 292	5 304 279 831	7 147 147 223	1 215 235 397	5 175 197 764	6 235 199 572	5 175 197 764	-5 34 29 209	3 104 129 303	6 165 140 303	-6 104 130 303	-6 104 130 303	
7 39 48 605	3 180 187 993	-5 111 101 477	3 168 70 414	-6 96 163 626	5 167 163 626	4 147 152 482	-5 34 29 209	3 104 129 303	6 165 140 303	-6 104 130 303	-6 104 130 303	
8 55 51 52879	4 184 182 193	-5 111 101 477	3 168 70 414	-6 96 163 626	5 167 163 626	4 147 152 482	-5 34 29 209	3 104 129 303	6 165 140 303	-6 104 130 303	-6 104 130 303	
9 68 72 727	6 188 72 727	0, K, 12	2 366 352 607	5 174 121 522	5 174 121 522	5 174 121 522	-5 34 29 209	3 104 129 303	6 165 140 303	-6 104 130 303	-6 104 130 303	
1, K, 12	1, K, 24	1, K, 12	2 366 352 607	5 174 121 522	5 174 121 522	5 174 121 522	-5 34 29 209	3 104 129 303	6 165 140 303	-6 104 130 303	-6 104 130 303	
2, K, 12	2, K, 24	2, K, 12	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	
3, K, 12	3, K, 14	3, K, 12	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	
4, K, 12	4, K, 14	4, K, 12	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	
5, K, 12	6, K, 14	5, K, 12	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	
6, K, 12	7, K, 14	6, K, 12	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	-5 35 44 295	
7, K, 12	8, K, 14	7, K, 12	-5									

## ON THE STRUCTURE OF PICROTOXIN. II.

Table 4 (cont.)

3, K, 3	3, K, 23	4, K, 12	4, K, 10	4, K, 5	4, K, 3
8 55 44 243	-6 39 56 977	-7 78 83 975	-7 39 50 758	-8 96 116 420	-8 64 82 29
-5 140 114 150	-5 39 50 758	-5 78 83 975	-5 39 50 758	-5 140 114 150	-5 140 114 150
3, K, 7	-4 130 97 354	5 134 144 897	-5 68 59 460	-6 229 184 874	-6 147 148 619
3 124 121 672	5 162 170 54	4 243 244 921	4 175 153 488	-5 55 47 480	
-7 68 93 296	4 68 69 926	6 78 81 160	5 55 68 122	5 162 143 968	4 100 140 213
5 55 95 802	7 96 101 516	6 88 91 122	5 162 143 968	5 104 143 261	
5 113 125 377		7 39 34 526	7 55 61 498	6 162 143 585	
4 229 259 6	3, K, 27	4, K, 16	4, K, 14	8 55 52 153	7 55 64 935
3 438 380 260			4, K, 9	8 55 56 125	
3 117 122 514	-5 55 45 217	-7 55 63 471	4, K, 7		
3 39 51 670	-5 39 47 500	-6 152 150 257			
6 184 168 197	3 55 66 869	-5 111 109 728	4 88 93 454	-7 117 136 670	-7 55 67 221
7 88 86 764	4 55 49 277	5 111 109 362	5 78 81 160	-6 124 119 907	
3, K, 11	3, K, 31	5 39 50 450	5 111 104 833	5 171 167 201	-5 269 253 830
7 39 42 943		7 39 51 9	6 39 51 9	5 200 188 552	
3, K, 11		4, K, 18	4, K, 13	6 78 72 62	
-7 68 83 720	3 55 53 186	4, K, 20	6 78 84 643	6 78 72 62	
16 96 104 860		4 147 145 600	4, K, 13		
5 222 249 924	4, K, 0				
-4 157 158 304	-5 88 95 90	4 147 145 600			
4 200 211 993	-5 88 82 0	4 55 59 264	5 178 77 51	-7 39 46 35	4, K, 11
5 141 129 790	4 104 99 500	6 39 47 883	4, K, 22	-5 55 61 514	-7 39 46 35
8 130 124 411	5 141 131 500	5 141 131 500	5 141 131 500	5 141 131 500	4 104 578
8 55 44 129	5 141 131 500	5 141 131 500	5 141 131 500	5 141 131 500	4 104 578
3, K, 15	3, K, 15	4, K, 24	-6 96 101 983	5 215 237 575	5 141 131 500
7 124 98 500	5 124 98 500	4 152 155 446	6 39 45 263	4 152 155 264	5 141 131 500
3 39 50 500	-5 55 69 443	5 133 93 200	7 39 46 386	6 96 100 33	
-7 39 38 26	4, K, 4	5 178 77 51	7 88 87 479		
-6 104 114 254		4, K, 2	4, K, 16		
-5 141 131 500	-7 86 106 332	4, K, 2	-7 39 43 511	4, K, 15	
-3 141 131 500	-8 88 105 592	4 104 103 353	-7 39 44 639	5 111 111 962	-7 35 60 46
3 242 248 816	5 130 118 460	-7 78 107 87	5 88 86 451	-6 147 134 211	
4 332 328 192	6 55 61 294	-6 238 259 172	7 88 81 550	6 147 134 211	
5 141 131 500	7 55 65 388	5 543 492 120	4, K, 1	6 83 204	
7 88 63 555	8 76 87 506	5 171 138 161	4, K, 21	5 124 118 442	
3, K, 19	3, K, 6	8 76 87 506	-8 39 35 832	-5 55 77 210	5 124 118 442
-7 96 110 671	4, K, 6	5 171 138 161	-5 55 77 210	6 83 82 417	
-3 124 114 150		4 136 122 265	6 39 53 74	7 39 43 826	
-5 88 86 451	-8 88 86 451	5 171 138 161	4, K, 19		
-4 147 131 210	9 188 194 631	-6 171 185 511	7 78 77 174	-6 39 41 151	
3 88 79 810	8 88 79 810	8 39 59 745	-5 55 51 743	5 55 71 747	
4 117 106 210	1 111 107 204	8 39 59 745	5 39 51 861	5 104 107 204	
5 88 75 410	8 76 61 229	8 39 59 745	6 88 87 980		
		6 166 164 987			

$$h_1 + h_2 + h_3 = 0 \quad (1)$$

and if

 $E_{h_1}$ ,  $E_{h_2}$ , and  $E_{h_3}$  are all large,

then the probability of

$$\varphi_{h_1} + \varphi_{h_2} + \varphi_{h_3} = 2\pi n \quad (2)$$

is high.  $\varphi_h$  is the phase of the structure factor  $E_h$ . This equation (2) corresponds to the equation

$$S_{h_1} \times S_{h_2} \times S_{h_3} \approx +1 \quad (3)$$

for the centrosymmetric case.  $S_h$  is the sign of the structure factor  $E_h$ .

It was decided to try to solve the structure using equation (2). As initial phases the following were chosen:

$h$	$k$	$l$	$E$	$\varphi$
1	4	0	2.27	0°
4	6	1	1.70	60°

The choice of parity groups for the initial phases has been discussed by Hauptman & Karle (1956). The choice of 140 and 461 was made since these two sets of indices could be combined by (2) with indices of large values of  $E$ . The phase of 461 was chosen equal to 60° to specify the enantiomorph.

Table 5. Comparison between bond lengths in  $\beta$ - and  $\alpha_1$ -bromopicrotoxinin

Standard deviations in both investigations: C-Br 0.015 Å, C-O 0.019–0.025 Å, C-C 0.021–0.027 Å.

Bond type	Br-C( $sp^3$ )	$\beta$ -Bromopicrotoxinin (this investigation)	$\alpha_1$ -Bromopicrotoxinin [from Craven's (1962) data]
O-C( $sp^3$ ) in 5-membered ring		O(1)—C(6) O(1)—C(8) O(4)—C(2) O(6)—C(3)	1.45 <sub>2</sub> 1.47 <sub>2</sub> 1.47 <sub>0</sub> 1.48 <sub>8</sub>
O-C and O=C in 5-membered lactone ring		O(4)—C(14) O(3)=C(14) O(6)—C(15) O(5)=C(15)	1.34 <sub>7</sub> 1.21 <sub>1</sub> 1.32 <sub>3</sub> 1.24 <sub>1</sub>
C—O and C—C in 3-membered ring		O(2)—C(12) O(2)—C(13) C(12)—C(13)	1.38 <sub>2</sub> 1.39 <sub>9</sub> 1.43 <sub>0</sub>
C( $sp^2$ )—C(epoxide)		C(13)—C(14)	1.50 <sub>4</sub>
C( $sp^3$ )—C(epoxide)		C(1)—C(13) C(11)—C(12)	1.51 <sub>4</sub> 1.54 <sub>6</sub>
C( $sp^3$ )—C( $sp^2$ )		C(5)—C(15)	1.49 <sub>2</sub>
C( $sp^3$ )—C( $sp^3$ )		C(1)—C(2) C(1)—C(6) C(1)—C(7) C(2)—C(3) C(3)—C(4) C(4)—C(5) C(4)—C(8) C(5)—C(6) C(6)—C(11) C(8)—C(9) C(8)—C(10)	1.54 <sub>0</sub> 1.55 <sub>1</sub> 1.50 <sub>3</sub> 1.54 <sub>1</sub> 1.52 <sub>1</sub> 1.50 <sub>7</sub> 1.57 <sub>6</sub> 1.54 <sub>8</sub> 1.56 <sub>7</sub> 1.50 <sub>6</sub> 1.52 <sub>5</sub> 1.53 <sub>5</sub>
		average	1.53 <sub>5</sub>

Forty phases were generated from these first phases, a new phase was included only if it had the same value indicated by more than one relation (2).

These 40 phases were now combined to give 450 phases; a new phase was included if it had a value indicated by one or the same value by several relations. Another 60 phases had indications of different values. These 60 phases were estimated by the weighted mean:

$$\varphi_h = \frac{\sum_i (E_{h_1}^t E_{h_2}^t) \varphi_i}{\sum_i E_{h_1}^t E_{h_2}^t}.$$

$\varphi_t$  is the phase found by the relation

$$\varphi_t + \varphi_{h_1}^t + \varphi_{h_2}^t = 0.$$

When the refinement was finished the values of the phases were compared, and the following average deviations were found.

	Average deviation from refined structure
All 510 phases	40°
The first 40 phases	21
The last 60 phases	40

Table 6. Comparison between valency angles in  $\beta$ - and  $\alpha_1$ -bromopicrotoxinin

Standard deviations are given for the  $\beta$  compound.

In the determination of the  $\alpha_1$  compound standard deviations ranging from 1.1° to 1.7° were found.

Angle	$\beta$ -Bromopicrotoxinin (this investigation)	$\alpha_1$ -Bromopicrotoxinin [from Craven's (1962) data]
C(6)—O(1)—C(8)	1.2°	107.0°
C(12)—O(2)—C(13)	1.3	61.9
C(2)—O(4)—C(14)	1.3	111.3
C(3)—O(6)—C(15)	1.3	106.0
C(2)—C(1)—C(6)	1.2	114.6
C(2)—C(7)	1.3	112.6
C(2)—C(13)	1.2	102.5
C(6)—C(7)	1.3	114.3
C(6)—C(13)	1.2	99.9
C(7)—C(13)	1.4	111.6
O(4)—C(2)—C(1)	1.1	106.4
O(4)—C(3)	1.2	109.1
C(1)—C(3)	1.2	113.5
O(6)—C(3)—C(2)	1.3	106.1
O(6)—C(4)	1.2	102.1
C(2)—C(4)	1.3	116.3
C(3)—C(4)—C(5)	1.2	97.5
C(3)—C(8)	1.3	125.5
C(5)—C(8)	1.3	99.7
C(4)—C(5)—C(6)	1.2	99.4
C(4)—C(15)	1.3	102.4
C(6)—C(15)	1.4	117.2
O(1)—C(6)—C(1)	1.2	109.9
O(1)—C(5)	1.3	100.2
O(1)—C(11)	1.3	115.8
C(1)—C(5)	1.2	115.6
C(1)—C(11)	1.3	104.1
C(5)—C(11)	1.3	111.8
O(1)—C(8)—C(4)	1.3	105.4
O(1)—C(9)	1.3	107.7
O(1)—C(10)	1.4	110.8
C(4)—C(9)	1.4	108.9
C(4)—C(10)	1.3	109.2
C(9)—C(10)	1.6	114.5
C(8)—C—Br	1.0	110.4
C(6)—C(11)—C(12)	1.5	99.9
O(2)—C(12)—C(11)	1.6	117.2
O(2)—C(13)	1.3	59.6
C(11)—C(13)	1.6	108.1
O(2)—C(13)—C(1)	1.6	119.7
O(2)—C(12)	1.3	58.5
O(2)—C(14)	1.6	119.0
C(1)—C(12)	1.6	111.3
C(1)—C(14)	1.5	107.4
C(12)—C(14)	1.7	134.3
O(3)=C(14)—O(4)	1.8	121.2
O(3)=C(13)	1.8	129.5
O(4)=C(13)	1.6	109.3
C(5)=C(15)—O(6)	1.9	120.0
C(5)=C(5)	1.8	129.1
O(6)=C(5)	1.4	110.8

A Fourier synthesis was calculated from the 510 phases.

From the Fourier map the position of the bromine atom was found. Light atoms were placed on 21 of the next highest peaks; 9 of these positions were later shown to be wrong. The 21 positions were chosen without chemical considerations to ensure the objectivity of the method. The structure could probably just as well have been solved from a three-dimensional Patterson synthesis.

Successive diagonal least-squares and Fourier calculations gave the positions of the 15 carbon atoms and the 6 oxygen atoms and an *R* value (observed reflexions only) of 0.17. The computations described so far were performed on the computer GIER. The Fourier program was a machine order program written by Lauesen (1964). The other computations were carried out using Algol programs written by Danielsen.\*

Anisotropic refinement by the program written by Gantzel, Sparks, Long & Trueblood (1967) was performed on the IBM 7090 computer at the NEUCC installation in Copenhagen. This reduced the *R* value to 0.11. In Table 2 the final geometric coordinates are shown, in Table 3 the final anisotropic temperature factors, and in Table 4 the observed and calculated  $|F|$  values.

### Description and discussion of the structure

The structure determination showed that  $\beta$ -bromopicrotoxinin and the  $\alpha_1$  isomer described by Craven (1962) are epimeric compounds. The difference between their configurations consists in the interchange of a  $\text{CH}_3$  group and a  $\text{CH}_2\text{Br}$  group at the asymmetric centre C(8). This result agrees with the conclusions drawn by Carman (1963) from a nuclear magnetic resonance study.

Comparisons between the two isomers are made in Fig. 1 and Tables 5, 6 and 7. The numbers given to the atoms are in accordance with the ones used by Craven (1962); note, however, that C(9) and C(10) are interchanged relative to Carman's notation. It is seen that in  $\beta$ -bromopicrotoxinin the bromine atom is attached to C(10), and C(9) is a methyl carbon, whereas the  $\alpha_1$  isomer has the bromine atom bonded to C(9), and C(10) is the methyl carbon. Fig. 1 shows the absolute configuration of the  $\beta$ -bromopicrotoxinin molecule. This has been assigned by comparison with the  $\alpha_1$  isomer for which the absolute configuration is known, and which must be sterically very closely related to the  $\beta$  isomer as inferred e.g. from the way the two compounds are synthesized. The knowledge of the absolute configuration of  $\beta$ -bromopicrotoxinin made it possible to assign the correct space group to the crystals, and  $P4_3$  had to be chosen instead of  $P4_1$  in order to obtain consistent configurations of the isomers.

\* D50, Program system for direct methods; D28, diagonal least-squares program; D45, stepwise minimization of the *R* value. Kemisk Institut, Aarhus Universitet.

Table 7. Comparison between some intramolecular non-bonded distances in  $\beta$ - and  $\alpha_1$ -bromopicrotoxinin

	$\beta$ -Bromopicrotoxinin (this investigation)	$\alpha_1$ -Bromopicrotoxinin (Craven, 1962)	3.30 Å
Br—C(4)	—	—	—
—C(9)	3.30 Å	—	—
—C(8)	2.90	2.98	—
—O(1)	3.24	3.41	—
C(2)—C(10)	3.25	3.18	—
C(7)—C(10)	3.56	3.36	—
—O(1)	2.85	2.86	—
—O(2)	2.86	2.77	—
C(15)—C(12)	3.15	3.18	—
—C(13)	3.03	3.11	—
—C(14)	3.26	3.34	—
O(5)—C(12)	3.29	3.29	—
—C(13)	3.51	3.56	—
—C(14)	3.66	3.70	—
—O(3)	4.07	4.29	—

The crystal structure determinations of both isomers appear to be of approximately the same accuracy as judged from the standard deviations given on bond lengths and valency angles which were calculated on the BONDLA program in the Crystal Structure Calculation System X-ray-63, from the University of Maryland, Computer Science Center.

In Table 5 are registered 27 pairs of equivalent bond lengths found in the two isomers. The difference between two equivalent bonds is in 14 cases less than the standard deviation ( $\sigma$ ) of the bond length in question as found in this investigation, in 8 cases less than  $2\sigma$  and in the remaining 5 cases less than  $3\sigma$ . All these differences may thus be considered insignificant. It is noticed that two of the largest discrepancies are found in the three-membered rings.

In Table 6, 51 pairs of chemically equivalent valency angles are recorded. In 33 cases the difference between two equivalent valency angles is less than  $\sigma$  (the standard deviation of the corresponding angle as found in this investigation), in 9 cases less than  $2\sigma$ , in 4 cases less than  $3\sigma$ , in 2 cases less than  $4\sigma$  and in the last three cases differences close to  $5\sigma$ ,  $6\sigma$  and  $8\sigma$  respectively are seen. These differences may be considered insignificant apart from the last named, in all of which the epimeric centre C(8) is involved, which will be discussed separately. Table 6 shows that rather big deviations from ideal valency angles are found in several cases as a consequence of the strain imposed by the fusion of several rings to form the complex skeleton of the bromopicrotoxinins. The most irregular arrangement of bonds is found at C(13). This is quite natural, since this carbon atom takes part in the formation of three rings, one three-membered and two five-membered. Another atom at which considerable strain is concentrated is C(4), as indicated primarily by large deviations of the three angles C-C(4)-C from  $109.5^\circ$ , but several angles C-C-C(4) are also appreciably affected.

In Table 7 comparison is made between some equivalent non-bonded interatomic distances in the two

epimers. In most cases only small deviations, less than 0·1 Å are found; these are however in a number of cases definitely significant. The different configuration of the two molecules must to some extent influence the surroundings of the atoms C(9), C(10) and Br, and actually deviations of about 0·2 Å between the distances C(7)-C(10) and between the distances Br-O(1)

are found. A similar deviation between the distances O(5)-O(3) indicates that the relative positions of the two carbonyl groups C(15)=O(5) and C(14)=O(3) are slightly different in the two compounds. This may probably be attributed to the packing of the molecules.

The molecular geometries of the main part of the two isomers therefore match very closely. The angular

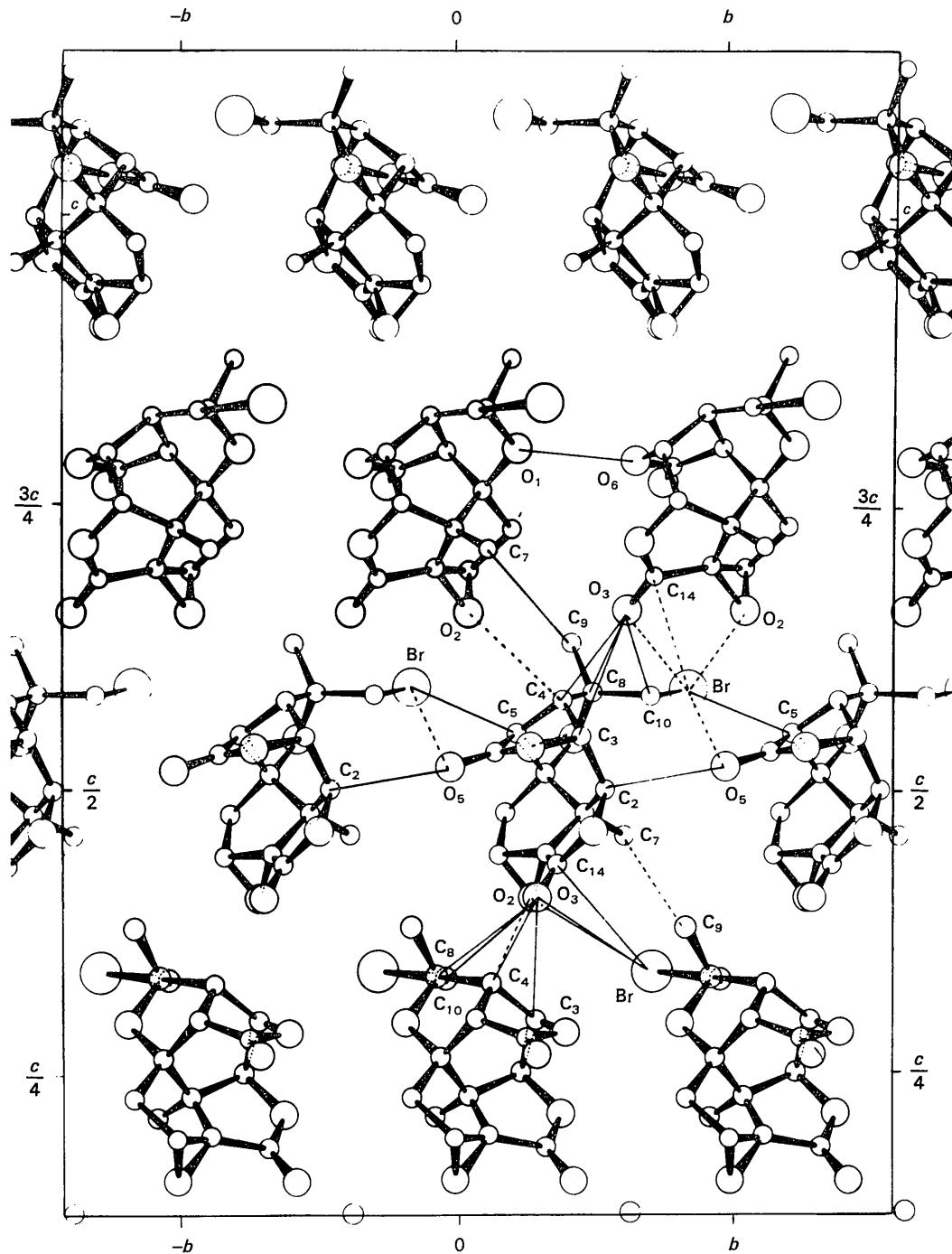


Fig. 2. The structure viewed along the  $a$  axis. Full lines and broken lines are used to distinguish between distances from the central molecule to neighbour molecules with common  $b$  and  $c$  coordinates but placed at different  $a$  levels (cf. Table 8).

Table 8. *Intermolecular distances*

The table comprises distances smaller than 3.6 Å involving only carbon and oxygen atoms and distances smaller than 4.0 Å involving the bromine atom.

I	$x$	, $y$	, $z$	V	$y$	, $\bar{x}+2$	, $z+\frac{1}{4}$
II	$x-1$	, $y$	, $z$	VI	$y+1$	, $\bar{x}+2$	, $z+\frac{1}{4}$
III	$x$	, $y+1$	, $z$	VII	$y+1$	, $\bar{x}+1$	, $z+\frac{1}{4}$
IV	$x-1$	, $y+1$	, $z$	VIII	$y$	, $\bar{x}+1$	, $z+\frac{1}{4}$
O(1)I	O(6)II		3.28 Å	C(9)I	C(7)VIII		3.58 Å
C(2)I	O(5)III		3.21	BrI	C(5)III		3.90 Å
C(3)I	O(3)VI		3.33	BrI	O(5)IV		3.84
C(4)I	O(3)VI		3.04	BrI	O(2)V		3.87
C(8)I	O(3)VI		3.47	BrI	O(3)V		3.80
C(10)I	O(3)VI		3.25	BrI	C(14)V		3.76
C(4)I	O(2)VII		3.49				

distribution at the epimeric centre, however, is significantly different in the two compounds. It is remarkable that the arrangement in  $\beta$ -bromopicrotoxinin is much more regular. In accordance with this it is evident from molecular models that the steric strain in this compound must be much smaller than in the  $\alpha_1$  isomer. A model of that compound suggests that the angles C(8)-C(9)-Br and C(4)-C(8)-C(9) should be expanded whereas the angle C(9)-C(8)-C(10) should be smaller than in regular tetrahedral arrangements; and significant deviations of these angles from 109.5° in the indicated directions are actually found. From such simple steric considerations it is not possible to explain why two more angles show deviations that are probably significant from 109.5°, i.e. in the  $\alpha_1$  isomer C(4)-C(8)-C(10) and in the  $\beta$  isomer C(9)-C(8)-C(10).

Further model considerations show that the conformation adopted by the  $\text{CH}_2\text{Br}$  group in the  $\beta$  isomer is undoubtedly the most favourable, but that this is apparently not the case with the  $\alpha_1$  isomer. In this compound it appears that a conformation with the bromine atom in a *trans* position relative to C(4) might give rise to less angular strain than the conformation found. One may expect that this conformation is present in the crystals of  $\alpha_2$ -bromopicrotoxinin; this is generally considered to be a polymorph of  $\alpha_1$ -bromopicrotoxinin, but the structure has not been determined.

The molecular packing is shown in Fig. 2. The roughly spherical molecule is surrounded by 14 neighbouring molecules, 6 at the same *c* level, 4 at each of the adjacent *c* levels. The shortest intermolecular contacts are listed in Table 8. The bromine atom approaches five carbon and oxygen atoms at distances 3.76–3.90 Å. In the crystal structure of the  $\alpha_1$  isomer similar distances were found (3.88–3.99 Å) but in that structure furthermore one very much shorter contact [3.37 Å between Br and O(2)] was observed. Craven suggested that this might possibly be interpreted as a

very weak intermolecular bonding interaction, but the present structure determination does not support this view. No particular short contacts between carbon and oxygen atoms are noticed. One distance [C(4)-O(3), 3.04 Å] is appreciably shorter than the other, but this has no similar short counterpart in the crystal structure of the  $\alpha_1$  isomer. Thus it appears that in both  $\beta$ - and  $\alpha_1$ -bromopicrotoxinin the intermolecular contacts are exclusively of the van der Waals' type.

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